

12 Part I: Multiple Choice. Write the correct answer in the space provided at the end of this section.

1. Determine the value of the absolute value expression $-7|-5 + 2|$.

(A) -49

(B) -21

(C) 21

(D) 49

$$\begin{aligned} &= -7|-3| \\ &= -7(3) \\ &= -21 \end{aligned}$$

2. If $(-3, -7)$ is on the graph of $y = f(x)$, what is the corresponding point on $y = |f(x)|$?

(A) $(-3, -7)$

(B) $(-3, 7)$

(C) $(3, -7)$

(D) $(3, 7)$

3. What is the range of $y = |-2x + 7|$?

(A) $\{y|y \in R\}$

(B) $\{y|y \geq -2, y \in R\}$

(C) $\{y|y \geq 0, y \in R\}$

(D) $\{y|y \geq 7, y \in R\}$

$$y \geq 0$$

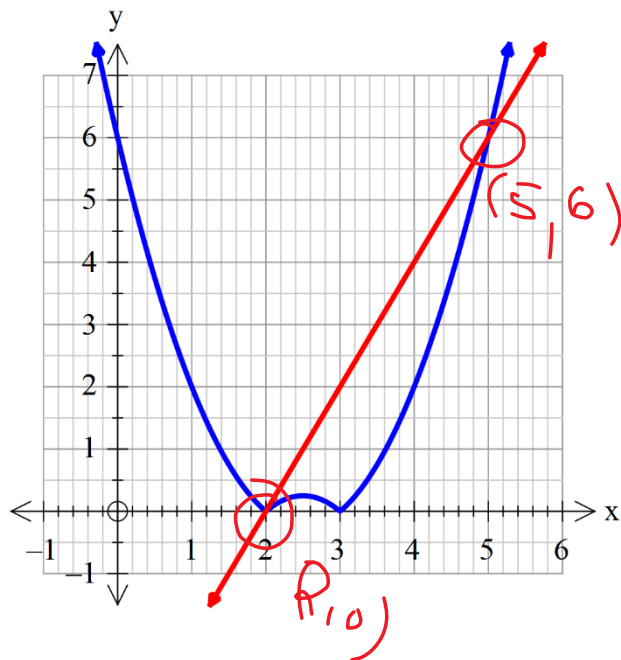
4. Which is a solution to the following?

(A) $(0, 2)$

(B) $(0, 6)$

(C) $(5, 6)$

(D) $(6, 5)$



5. Solve $|3x - 6| = 4x$

(A) ~~$x = -6$~~

(B) ~~$x = -6$~~ and $x = \frac{6}{7}$

(C) $x = \frac{6}{7}$

(D) no solution

$|3(\frac{6}{7}) - 6| = 4(\frac{6}{7})$
 $|\frac{18}{7} - \frac{42}{7}| = \frac{24}{7}$
 $|\frac{-24}{7}| = \frac{24}{7}$
 $\frac{24}{7} = \frac{24}{7}$

6. What is the invariant point for the function $y = |2x - 6|$?

(A) -6

(B) $\frac{1}{3}$

(C) 2

(D) 3

$2x - 6 = 0$
 $\frac{2x}{2} = \frac{6}{2}$
 $x = 3$

7. Solve $|3x + 2| + 4 = 1$?

(A) $-\frac{5}{3}$

(B) $-\frac{5}{3}$ and $\frac{1}{3}$

(C) $\frac{1}{3}$

(D) no solution

$|3x + 2| = 1 - 4$
 $|3x + 2| = -3$

8. What are the invariant points on $y = 2x + 5$ if its reciprocal, $y = \frac{1}{2x+5}$, is also graphed?

(A) (-3, -2)

(B) (-2, -3)

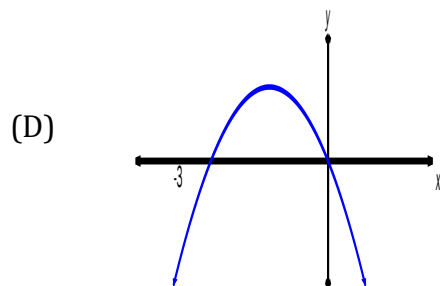
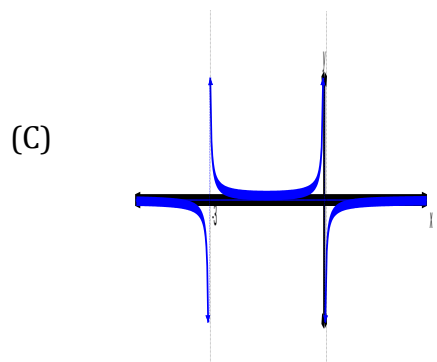
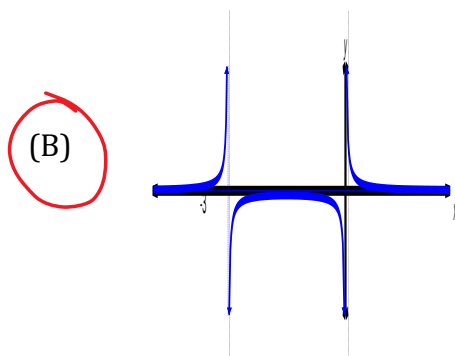
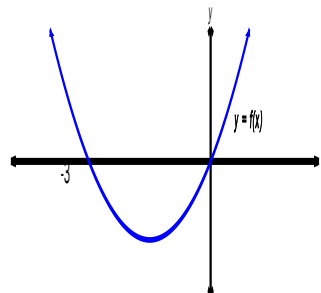
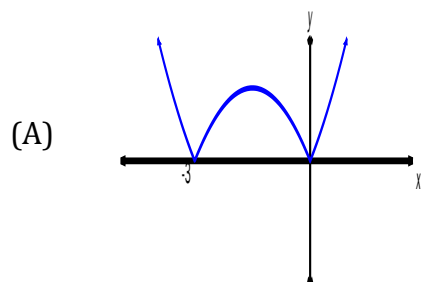
(C) (-2, 1), (-3, -1)

(D) (1, -2), (-1, -3)

$2x + 5 = -1$
 $2x = -1 - 5$
 $\frac{2x}{2} = \frac{-6}{2}$
 $x = -3$
 $(-3, -1)$

$2x + 5 = 1$
 $2x = 1 - 5$
 $\frac{2x}{2} = \frac{-4}{2}$
 $x = -2$
 $(-2, 1)$

9. Given the graph of $y = f(x)$, which graph is its reciprocal?



10. What is the equation of the vertical asymptote for the reciprocal of $y = -5x - 9$?

- (A) $x = -\frac{9}{5}$
- (B) $x = -\frac{5}{9}$
- (C) $x \neq -\frac{9}{5}$
- (D) $x \neq -\frac{5}{9}$

$$\begin{array}{l}
 5x - 9 \neq 0 \\
 -5x \neq 9 \\
 \hline
 -5 \quad -5 \\
 \hline
 x \neq -\frac{9}{5} \\
 \hline
 \text{VA} \\
 x = -\frac{9}{5}
 \end{array}$$

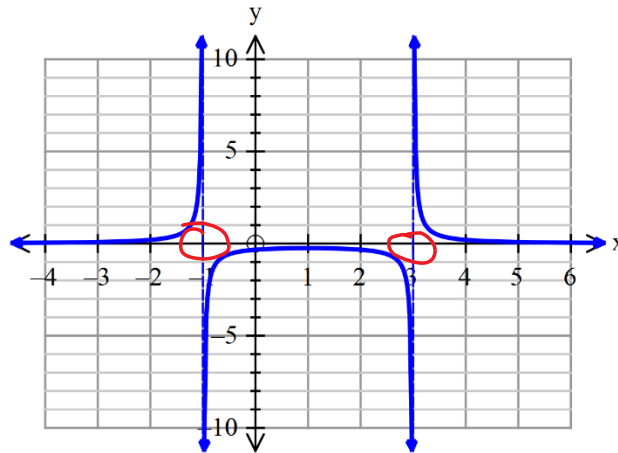
11. What is the y-intercept of the reciprocal of $y = 2x^2 - 5x + 6$?

- (A) 0
- (B) $\frac{1}{6}$
- (C) 6
- (D) undefined

12. The graph shown represents the reciprocal of which quadratic function?

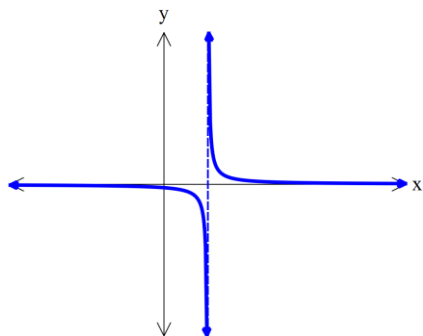
- (A) $f(x) = x^2 - 4x + 3$
- (B) $f(x) = x^2 - 2x - 3$
- (C) $f(x) = x^2 + 2x - 3$
- (D) $f(x) = x^2 + 4x + 3$

$$\begin{array}{l}
 x = -1, x = 3 \\
 (x + 1)(x - 3) \\
 x^2 - 2x - 3
 \end{array}$$

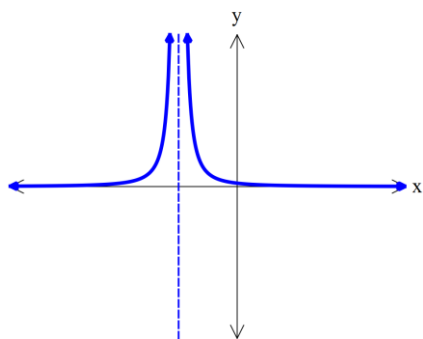


13. Which is the graph of the reciprocal of a quadratic function with discriminant 0?

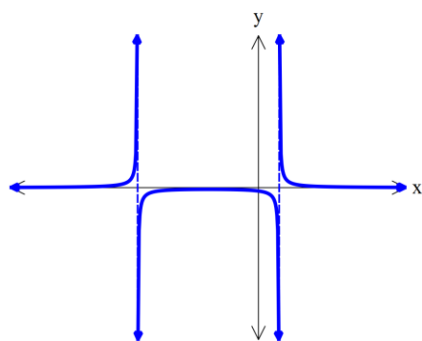
(A)



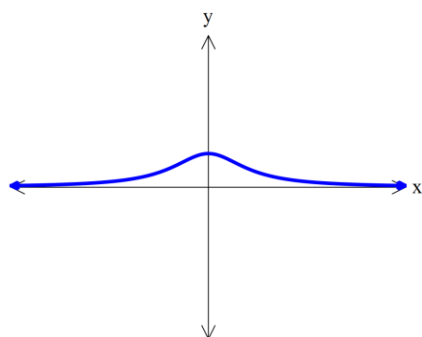
(B)



(C)



(D)



Answers to multiple choice.

1.____ 2.____ 3.____ 4.____ 5.____

6.____ 7.____ 8.____ 9.____ 10.____

11.____ 12.____ 13.____

18 **Part II: Constructed Response. Answer each question in the space provided. Show all workings.**

14. Evaluate:

2 (A) $|-3| - |-7|$

$$= 3 - 7$$
$$= -4$$

2 (B) $-2 - 4|5 + (-8)|$

$$= -2 - 4|-3|$$
$$= -2 - 4(3)$$
$$= -2 - 12$$
$$= -14$$

2 (C) $|-2 - 2(2 - 5)^2 + 6|$

$$= |-2 - 2(-3)^2 + 6|$$
$$= |-2 - 2(9) + 6|$$
$$= |-2 - 18 + 6|$$
$$= |-14|$$
$$= 14$$

3

12. Express as a piecewise function: $y = |4x - 12|$

$$4x - 12 = 0 \quad \leftarrow \begin{array}{c} 0 \quad 4 \\ \hline \end{array}$$

$$\frac{4x}{4} = \frac{12}{4} \quad y = 4(0) - 12 \quad y = 4(4) - 12$$

$$x = 3 \quad y = -12 \quad y = 16 - 12$$

$$\quad \quad \quad y = -12 \quad y = 4$$

$$y = \begin{cases} 4x - 12, & x \geq 3 \\ -(4x - 12), & x < 3 \end{cases}$$

4

13. Solve algebraically:

$$|x^2 - 4| = 3x$$

Case 1:

$$x^2 - 4 = 3x$$

$$x^2 - 3x - 4 = 0$$

$$(x + 1)(x - 4)$$

$$\cancel{x = -1}, x = 4$$

Check:

$$x = -1$$

$$|(-1)^2 - 4| = 3(-1)$$

$$|1 - 4| \neq -3$$

$$x = 4$$

$$|4^2 - 4| = 3(4)$$

$$|16 - 4| = 12$$

$$|12| = 12$$

$$12 = 12 \checkmark$$

Case 2:

$$-(x^2 - 4) = 3x$$

$$-x^2 + 4 - 3x = 0$$

$$x^2 + 3x - 4 = 0$$

$$(x - 1)(x + 4)$$

$$x = 1, x = -4$$

$$x = 1$$

$$|1^2 - 4| = 3(1)$$

$$|1 - 4| = 3$$

$$|-3| = 3$$

$$3 = 3 \checkmark$$

$$|(-4)^2 - 4| = 3(-4)$$

$$|16 - 4| \neq -12$$

- 5 14. Algebraically determine the invariant points, equations of asymptotes, and x - and y -intercepts for the functions $f(x) = 2x + 5$ and $y = \frac{1}{f(x)}$.

Sketch both graphs on the same set of axes.

$$g(x) = \frac{1}{2x+5}$$

$$2x+5 \neq 0$$

$$2x \neq -5$$

$$x \neq -\frac{5}{2}$$

$$\text{VA: } x = -\frac{5}{2} = -2.5$$

$$2x+5 = -1$$

$$2x = -1-5$$

$$\frac{2x}{2} = \frac{-6}{2}$$

$$x = -3$$

$$(-3, -1)$$

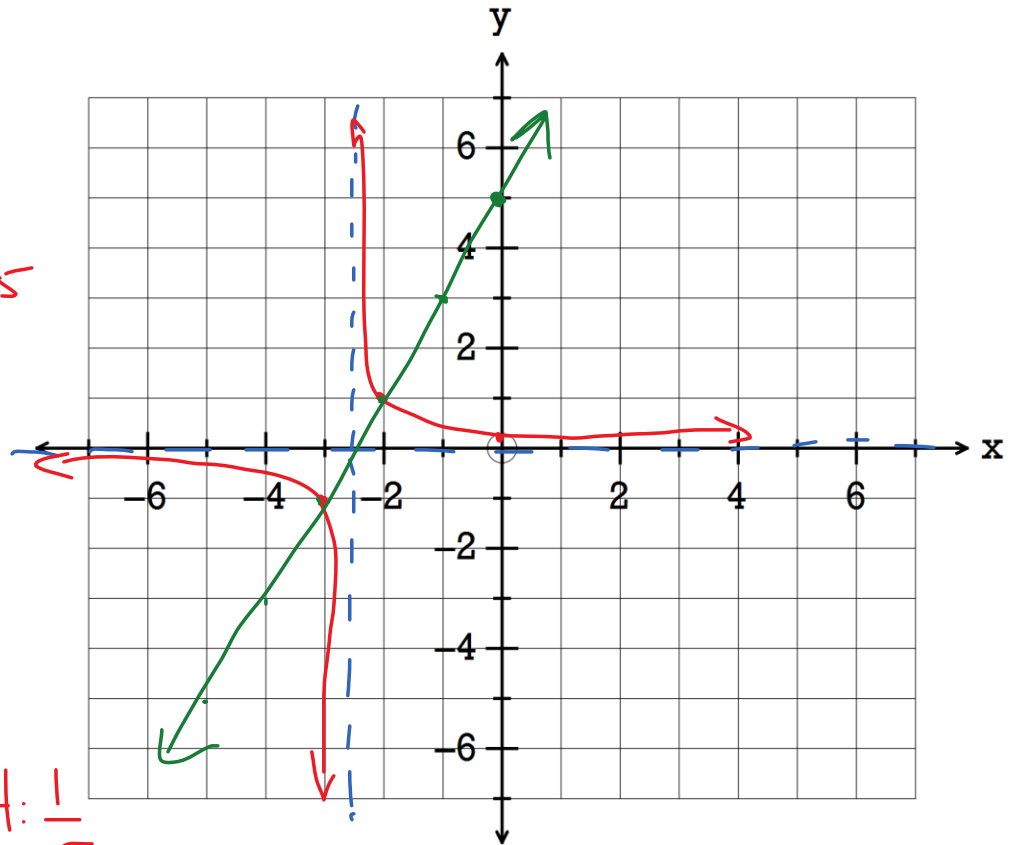
$$2x+5 = 1$$

$$2x = 1-5$$

$$\frac{2x}{2} = \frac{-4}{2}$$

$$x = -2 \quad (-2, 1)$$

$$y\text{-int: } \frac{1}{5}$$



15. Graph the function $f(x) = x^2 + x - 6$ and its reciprocal.

$$g(x) = \frac{1}{x^2 + x - 6}$$

$$x^2 + x - 6 \neq 0$$

$$(x-2)(x+3) \neq 0$$

$$x \neq 2, x \neq -3$$

$$VA: x=2, x=-3$$

$$x^2 + x - 6 = 1$$

$$x^2 + x - 6 - 1 = 0$$

$$x^2 + x - 7 = 0$$

$$x = \frac{-1 \pm \sqrt{(1)^2 - 4(1)(-7)}}{2(1)}$$

$$2(1)$$

$$x = \frac{-1 \pm \sqrt{29}}{2}$$

$$x = \frac{-1 \pm 5.4}{2}$$

$$x = -3.2 \quad x = 2.2$$

$$(-3.2, 1) \quad (2.2, 1)$$

$$x^2 + x - 6 = -1$$

$$x^2 + x - 6 + 1 = 0$$

$$x^2 + x - 5 = 0$$

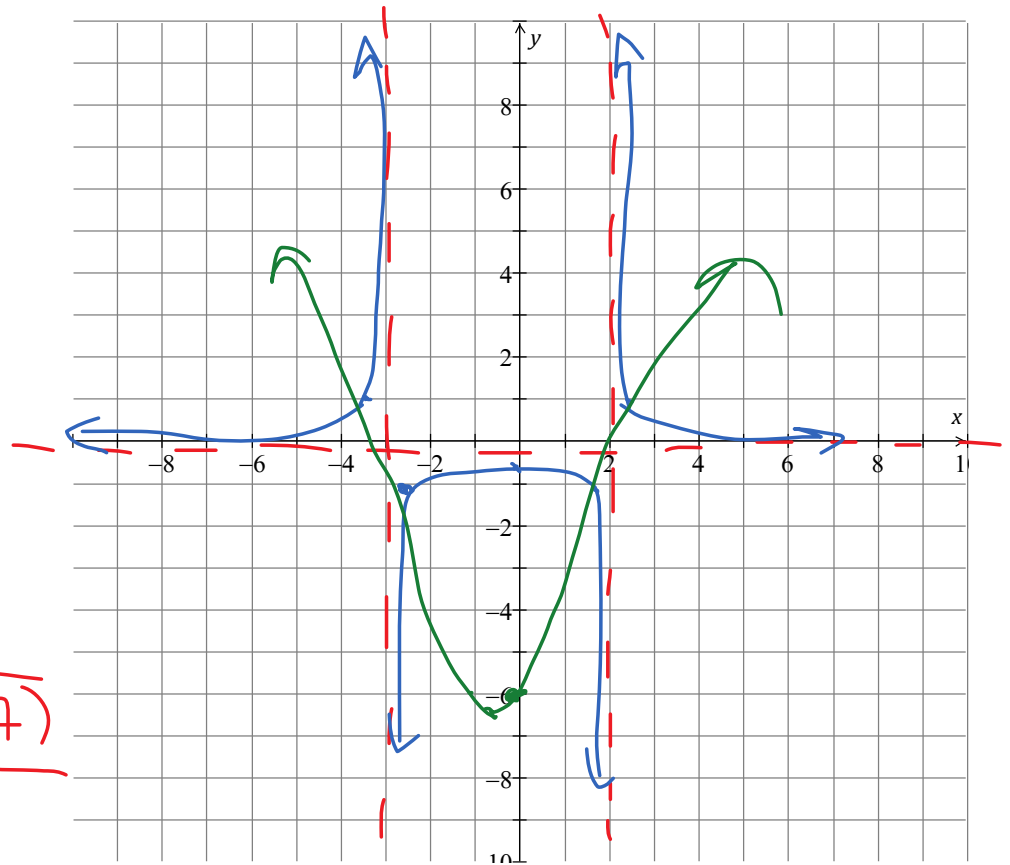
$$x = \frac{-1 \pm \sqrt{(1)^2 - 4(1)(-5)}}{2(1)}$$

$$x = \frac{-1 \pm \sqrt{21}}{2}$$

$$x = \frac{-1 \pm 4.6}{2}$$

$$x = -2.8 \quad x = 1.8$$

$$(-2.8, -1) \quad (1.8, -1)$$

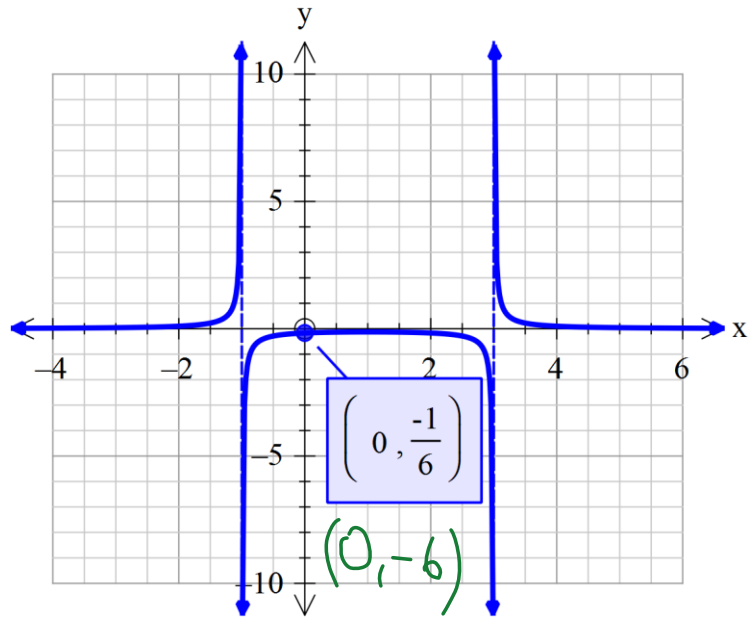


$$p = -\frac{b}{2a} = -\frac{1}{2(1)} = -0.5$$

$$q = (-0.5)^2 + (0.5) = -6.25$$

$$(-0.5, -6.25)$$

16. Given the following graph of a reciprocal function, determine the original function and sketch its graph.



$$x = -1, x = 3$$

$$y = a(x+1)(x-3)$$

$$-6 = a(0+1)(0-3)$$

$$\frac{-6}{-3} = \frac{-3a}{-3}$$

$$a = 2$$

$$y = 2(x+1)(x-3)$$

$$y = 2(x^2 - 2x - 3)$$

$$y = 2x^2 - 4x - 6$$

$$p = \frac{-(-4)}{2(2)} = \frac{4}{4} = 1$$

$$q = 2(1)^2 - 4(1) - 6 = -8$$

$(1, -8)$

