

Part I: Multiple Choice. Write the correct answer in the space provided at the end of this section.

1. Observe the following graph.

In which quadrant does the graph begin?

- (A) 1
- (B) 2
- (C) 3
- (D) 4

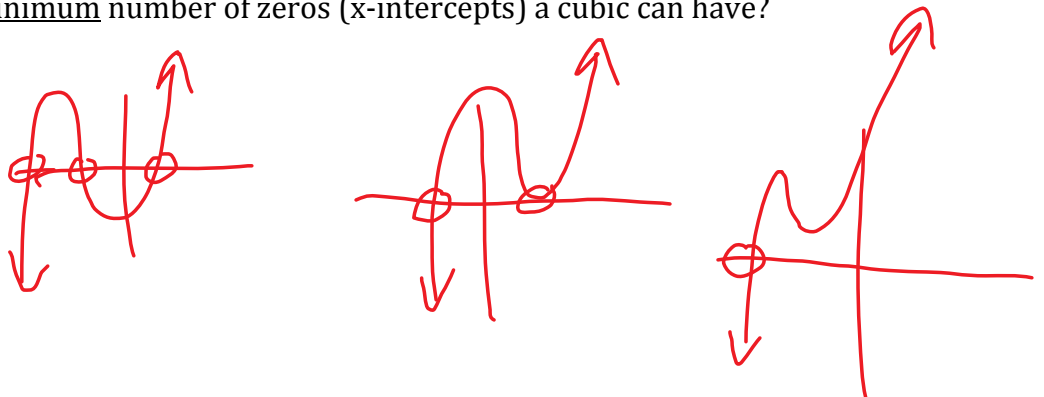


2. The graph of the function $p(x) = x^3 + 6x^2 + 11x + 6$ will cross the y-axis at?

- (A) 0
- (B) 1
- (C) 6
- (D) 11

3. What is the minimum number of zeros (x-intercepts) a cubic can have?

- (A) 0
- (B) 1
- (C) 2
- (D) 3



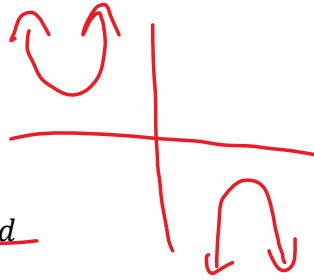
4. For the graph of which of the following functions, would it be possible to have NO x-intercepts?

~~(A) $y = ax^3$~~

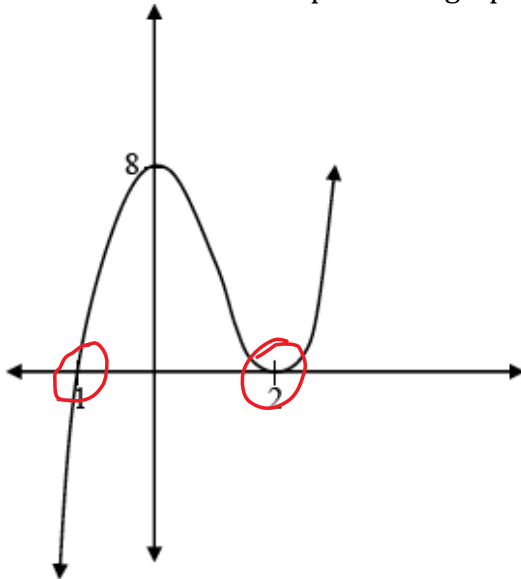
~~(B) $y = ax + b$~~

(C) $y = ax^2 + bx + c$

~~(D) $y = ax^3 + bx^2 + cx + d$~~



5. What are the x-intercepts of the graph below?



(A) 0 and 8

(B) -1 and 2

(C) 1 and -2

(D) 0 and -8

6. What is the degree of the polynomial function: $f(x) = \frac{1}{2}x^3 + 6x - 4$?

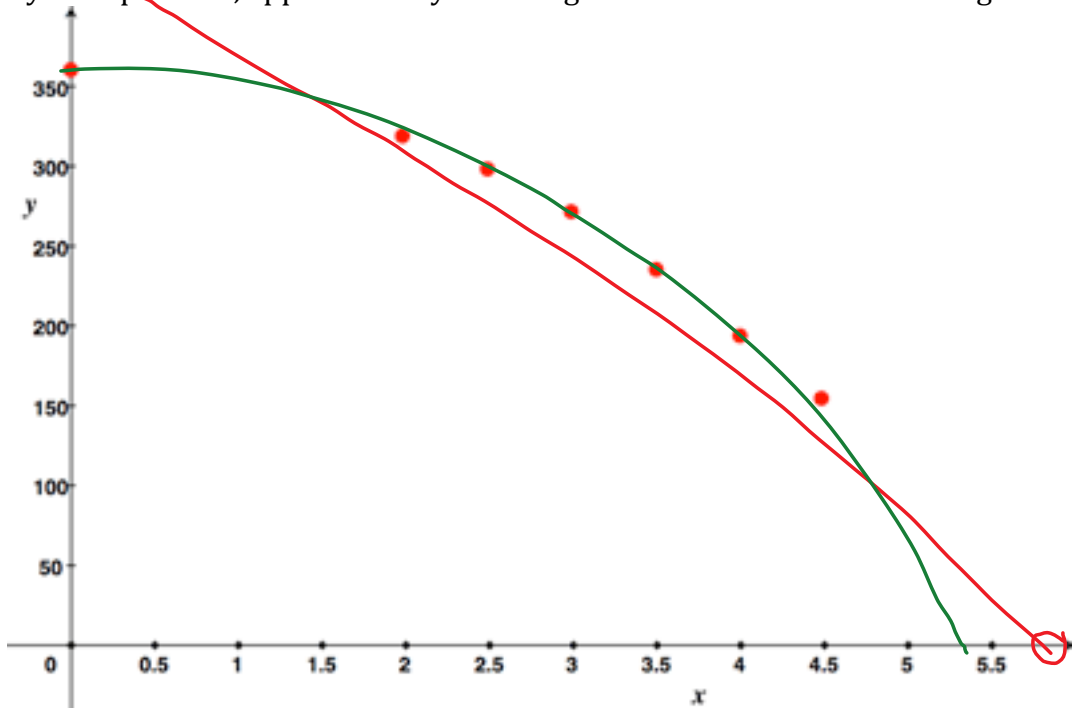
(A) 0

(B) 1

(C) 2

(D) 3

7. By extrapolation, approximately how long will it take the ball to hit the ground?



- (A) 4.5 s
- (B) 5
- (C) 5.5
- (D) 6

8. The graph of a polynomial function with a leading coefficient of $-3x^3$ will have an end behavior of:

- (A) Q2 → Q1
- (B) Q2 → Q4
- (C) Q3 → Q1
- (D) Q3 → Q4



9. Determine the degree of the polynomial function: $f(x) = x^2(x - 2x + 1)$

- (A) 0
- (B) 1
- (C) 2
- (D) 3

$$f(x) = x^2(-x + 1)$$

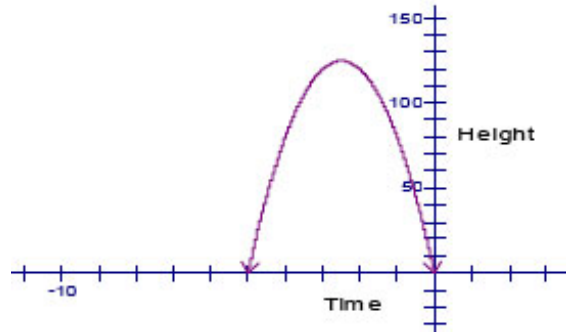
$$f(x) = -x^3 + x^2$$

Handwritten red work showing the expansion of the polynomial function. The first line is $f(x) = x^2(-x + 1)$ with arrows pointing from the x^2 term to $-x$ and 1 . The second line is $f(x) = -x^3 + x^2$, with a circled '3' under the x^3 term.

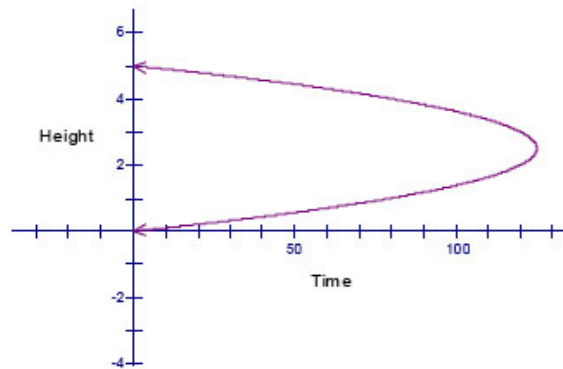
10. You throw a ball and measure its height at different times. You record the time and height in a table of values (shown below). The time is in seconds and the height is in centimeters.

Time (s)	Height (cm)
0	0
1	80
2	120
3	120
4	80
5	0

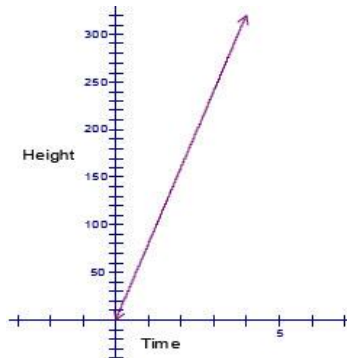
(A)



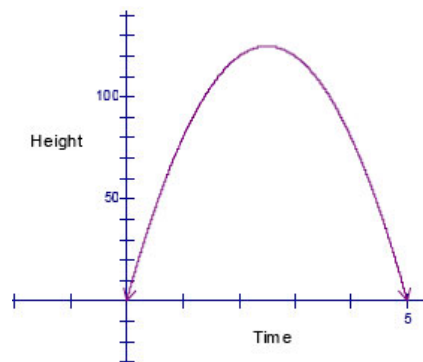
(B)



(C)

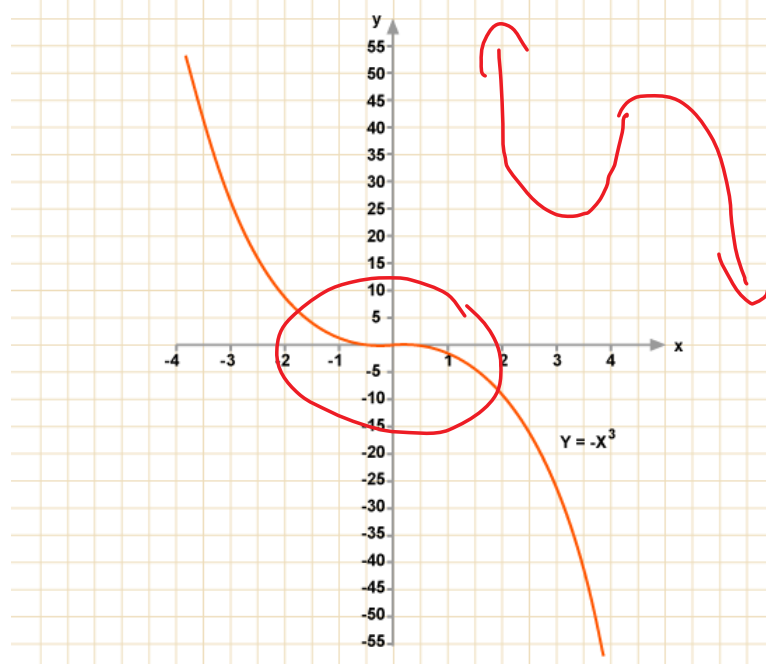


(D)



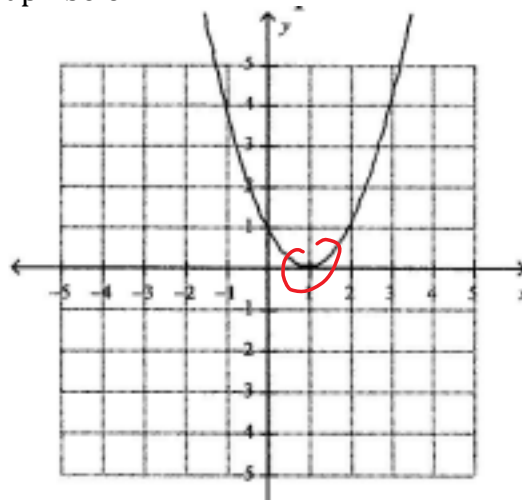
11. Determine the number of turning points in the following graph?

- (A) 0
- (B) 1
- (C) 2
- (D) 3



12. Determine the equation of the graph below:

- (A) $f(x) = -x^2 - 3x - 1$
- (B) $g(x) = x^2 - 2x + 1$
- ~~(C) $h(x) = x^3 - 2x^2 + 1$~~
- ~~(D) $j(x) = -x^3 + 2x$~~



13. How many x-intercepts does the graph from #12 have?

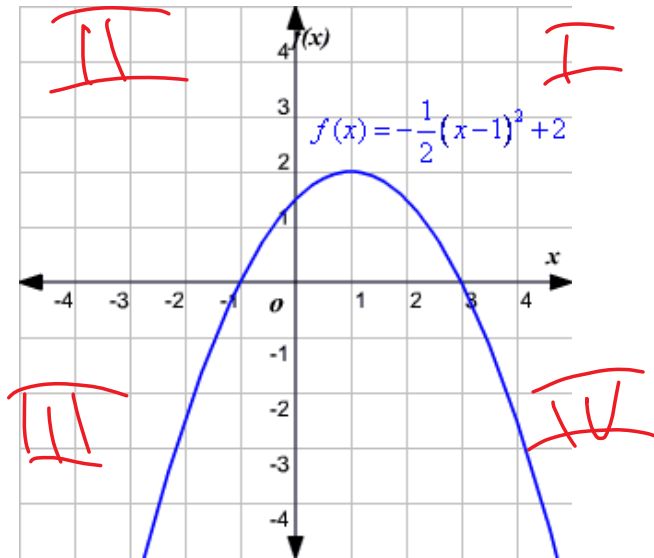
- (A) 0
- (B) 1
- (C) 2
- (D) 3

14. What is the range of the graph shown in #12?

- (A) $\{y|y \geq 1, y \in \mathbb{R}\}$
- (B) $\{y|y \geq 0, y \in \mathbb{R}\}$
- (C) $\{y|y \leq 1, y \in \mathbb{R}\}$
- (D) $\{y|y \leq 0, y \in \mathbb{R}\}$

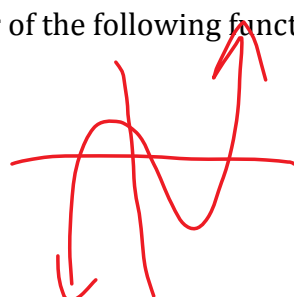
15. Describe the end behavior of the graph below:

- (A) Q1 to Q2
- (B) Q4 to Q2
- (C) Q2 to Q4
- (D) Q3 to Q4



16. Describe the end behavior of the following function: $f(x) = 2x^3 + x^2 - 2x + 7$

- (A) Q2 to Q1
- (B) Q2 to Q4
- (C) Q3 to Q2
- (D) Q3 to Q1



17. The growth of a tree can be modeled by the function $h(t) = 2.3t - 0.45$ where h represents the height in metres and t represents the time in years. Approximately how long will it take the tree to grow 32 m tall?

- (A) 13 years
- (B) 14 years
- (C) 15 years
- (D) 16 years

$$32 = 2.3t - 0.45$$

$$t = 14$$

18. Determine the equation of the linear regression function for the data:

x	1	2	3	4	5	6
y	84	155	241	310	405	478

- (A) $y = 79.7x - 0.07$
- (B) $y = 78.1x - 1.07$
- (C) $y = 79.7x + 0.07$
- (D) $y = 78.1x + 1.07$

Lin Reg

$$y = ax + b$$

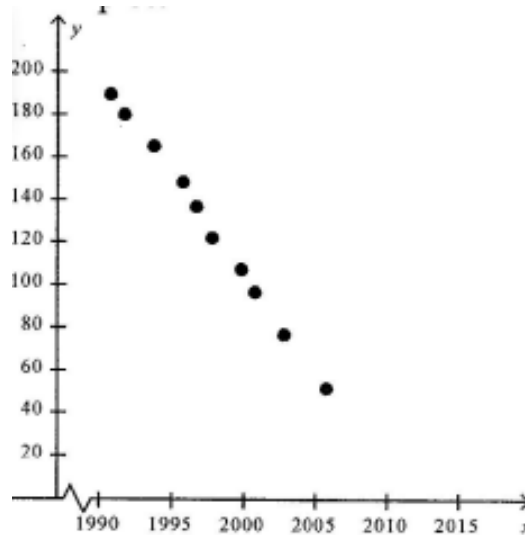
$$a = 79.68571429$$

$$b = -0.066666667$$

$$y = 79.7x - 0.07$$

19. What kind of relationship might there be between the independent and dependent scatter plot?

- (A) linear
- (B) quadratic
- (C) cubic
- (D) neither



20. Use cubic regression to interpolate the value of when $x = 5$

x	1	2	3	4	6	7	8	9
y	12.4	30.3	41.1	55.7	68.9	83.0	101.3	125.5

- (A) 61
- (B) 62
- (C) 63
- (D) 64

$$a = 0.356$$

$$b = -4.85$$

$$c = 30.3$$

$$d = -13.8$$

$$y = 0.356x^3 - 4.85x^2 + 30.3x - 13.8$$

$$y = 0.356(5)^3 - 4.85(5)^2 + 30.3(5) - 13.8$$

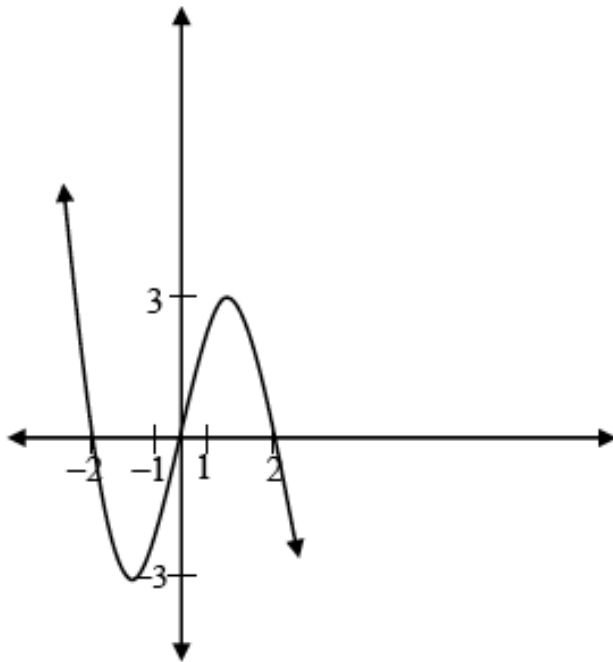
$$y = 61$$

Answers to multiple choice.

- 1.____ 2.____ 3.____ 4.____ 5.____
 6.____ 7.____ 8.____ 9.____ 10.____
 11.____ 12.____ 13.____ 14.____ 15.____
 16.____ 17.____ 18.____ 19.____ 20.____

15 Part II: **Constructed Response. Answer each question in the space provided. Show all workings.**

5 21. Use the following graph to fill in the table:



Type of Function:	cubic
Degree:	3
x-intercepts:	-2, 0, 2
y-intercepts:	0
Domain:	$\{x x \in \mathbb{R}\}$
Range:	$\{y y \in \mathbb{R}\}$
Sign of Leading Coefficient	-ve
Number of Turning Points:	2
End Behaviour:	rise (fall) fall (rise) Q II \rightarrow Q IV

- 2 22. Does the point $(2, 5)$ lie on the graph of $f(x) = x^3 - 4x + 9$?

$$5 = (2)^3 - 4(2) + 9$$

$$5 = 8 - 8 + 9$$

$$5 \neq 9$$

NO!

- 3 23. The motion of a motorized vehicle along a straight path is given by the function $m = t^3 - 23t^2 + 24t + 8$, where m is the displacement of the vehicle in millimeters and t is the time in seconds, $t \geq 0$. Determine the displacement of the vehicle after 62 seconds.

$$m = (62)^3 - 23(62)^2 + 24(62) + 8$$

$$m = 151412 \text{ mm}$$

- 5 24. Determine the following characteristics of the polynomial function $f(x) = 5x^2 + 3x - 4$.

- # of x-intercepts

2

- end behavior

rise left / rise right $QII \rightarrow QI$



- domain

$\{x | x \in \mathbb{R}\}$

- range

$$p = \frac{-b}{2a} = \frac{-3}{2(5)} = -0.3$$

$$q = 5(-0.3)^2 + 3(-0.3) - 4 = -4.65$$

$\{y | y \geq -4.65\}$

- number of possible turning points

1