$\qquad$

### 2.4 Angle Properties in Polygons

A concave polygon is defined as a polygon with one or more interior angles greater than $180^{\circ}$.

concave polygon

A convex polygon is defined as a polygon with all its interior angles less than $180^{\circ}$.

convex polygon

The focus of this chapter, however, will be on convex polygons. We will now discover the relationship between the sum of the interior angles and the number of sides in a convex polygon using the angle sum property. You already know that the sum of the angles in a triangle is $180^{\circ}$.

If we separate each polygon into triangles by drawing diagonals we can then use the following table to make our conjecture. Each vertex of a triangle must be a vertex of the original polygon.

| Number of <br> Sides | Diagram | Number of <br> Triangles <br> Formed | Sum of <br> Angles |
| :--- | :--- | :--- | :--- |
| 4 |  | 2 | $360^{\circ}$ |
| 5 |  |  |  |
| 6 |  |  |  |

The focus of this investigation is for you to recognize that the sum of the angles increases by $180^{\circ}$ as the number of sides increase by one.

| Name | Number of Sides | Number of Triangles in Diagram | Sum if Interior Angles |
| :---: | :---: | :---: | :---: |
| Triangle | 3 | 1 | $180^{\circ}$ |
| Quadrilateral | 4 | $2$ | $360^{\circ}$ |
| Pentagon | 5 | $S$ | $540^{\circ}$ |
| Hexagon | 6 |  | $720$ |
| Heptagon | 7 | $5$ | $900^{\circ}$ |
| Octogon | 8 | 0 | 1080 |

Make a conjecture about the relationship between the sum of the measures of the interior angles of a polygon, $S$, and the number of sides of the polygon, $n$.


Example 1:
Determine the sum of the measures of the interior angles of a regular 15 sided figure.

$$
n=15
$$

$$
S=180(n-2)
$$



$$
S=?
$$

$$
S=180(15-2)
$$

$$
S=180(13)
$$

$$
S=2340^{\circ}
$$

Example 2:
The sum of the interior angles in a regular polygon is $1980^{\circ}$. Determine the number of sides in the figure.


$$
\begin{aligned}
& S=180(n-2) \\
& \frac{1980^{\circ}}{180^{\circ}}=\frac{180^{\circ}(n-2)}{180^{\circ}} \\
& 11=n-2 \\
& 11+2=n \\
& n=13
\end{aligned}
$$

## Example 3:

In baseball, the home plate is shaped like the one shown. It has 3 right angles and 2 other congruent angles ( A and B ). Find the measures of $\angle A$ and $\angle B$.
$S=180(n-2)$

$S=$
$180(5-2)$

$$
=540^{\circ}-270^{\circ}
$$

$S=180(3)$
$S=540^{\circ}$


## Regular Polygons

For a regular polygon, where all sides equal, all angles will be equal.

## Example 4:

(A) Determine the sum of the interior angles in an 18 sided regular polygon.

$$
\begin{array}{ll}
n=18 & S=180(n-2) \\
S=7 & S=180(18-2) \\
& S=180(16) \\
& S=2880^{\circ}
\end{array}
$$

(B) Determine the measure of each individual interior angle in this polygon.


Textbook Questions: page 99-100 \#1, 2, 3, 6, 7a

