

2.6 Proving Congruent Triangles

Here you will focus on formal geometric proofs. Where applicable, it would be beneficial to draw diagrams so that you can have a visual representation of what is given and can determine other relationships.

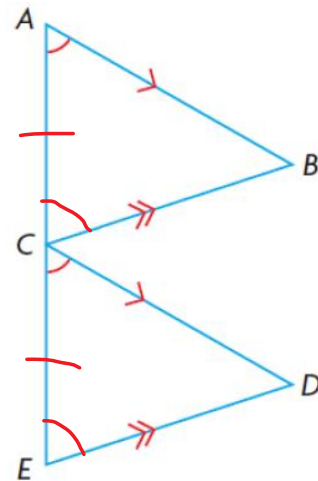
Remember, when you prove two triangles are congruent, their corresponding parts are congruent.

Example 1:

Given $AC = CE$

Prove $\triangle ABC \cong \triangle CDE$

| Statement | Reason |
|-------------------------------------|----------------------|
| $AB \parallel CD$ | Given |
| $\angle CAB = \angle ECB$ | Given |
| $\angle BCA = \angle DEC$ | corresponding angles |
| $\triangle ABC \cong \triangle CDE$ | ASA |



Example 2:

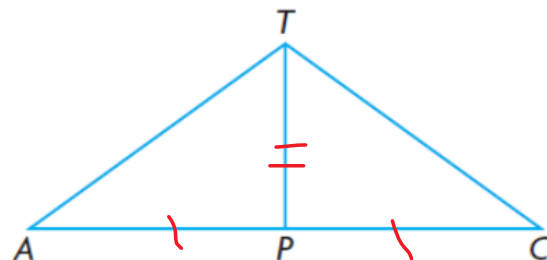
Given $TP \perp AC$

$AP = CP$

Prove $\triangle TAC$ is isosceles.

\perp : perpendicular
(meets at 90°)

| Statement | Reason |
|---------------------------------|----------------------------------|
| $AP = CP$ | Given |
| $\angle APT = 90^\circ$ | $TP \perp AC$ |
| $\angle CPT = 90^\circ$ | |
| $TP = TP$ | Common side |
| $\triangle TAP = \triangle TCP$ | SAS |
| $TA = TC$ | matching sides |
| $\triangle TAC$ is isosceles | 2 sides in a triangle are equal. |



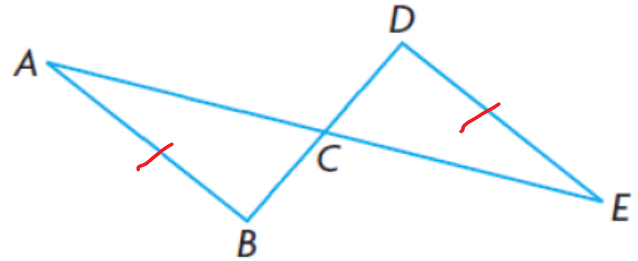
Example 3:

Given: AE and BD bisect each other at C .

$$AB = ED$$

Prove: $\angle A = \angle E$

| Statement | Reason |
|-------------------------------------|--|
| $AB = ED$ | Given |
| $AC = EC$ $BC = DC$ | AE and BD bisect each other at C . (given) |
| $\triangle ABC \cong \triangle EDC$ | SSS |
| $\angle A = \angle E$ | Matching angles of congruent triangles |



Example 4:

Given: $BC = CD$

AC bisects $\angle BCD$

Prove: $\triangle ABC \cong \triangle ADC$

| Statement | Reason |
|-------------------------------------|------------------------|
| $\overline{BC} = \overline{CD}$ | Given |
| $\angle BCA = \angle DCA$ | $\angle C$ is bisected |
| $\overline{AC} = \overline{AC}$ | Common side |
| $\triangle ABC \cong \triangle ADC$ | SAS |

