

8.5 Similar Objects: Scale Models and Scale Diagrams

We will now extend our knowledge of scale factors and scale diagrams of 2-D shapes to scale factors and scale diagrams of 3-D objects.

We will use a scale factor to determine unknown measurements of similar 3-D objects.

At the end of the section we will be able to use a given scale factor to determine the unknown dimensions of a 3-D object.

Similar Objects - Two or more 3-D objects that have proportional dimensions.

Example 1:

The dimensions of a scale drawing of a patio chair are 2 cm by 1.5 cm by 4 cm, and a scale factor of 1:30 is applied. Determine the actual dimensions of the patio chair.

$$2 \text{ cm} \times 30 = \underline{60 \text{ cm}}, \quad 1.5 \text{ cm} \times 30 = \underline{45 \text{ cm}},$$

or

$$4 \text{ cm} \times 30 = \underline{120 \text{ cm}}$$

$$k = \frac{\text{scale}}{\text{original}}$$

$$\frac{1}{30} = \frac{2}{x}$$

$$x = 2(30)$$

$$x = 60 \text{ cm}$$

Example 2:

During an Art class, students are projecting the image of a can of Carnation milk on the wall. The projector applies a scale factor of 250%. If the can has a diameter of 10 cm and a height of 12.5 cm, what are the dimensions of the image on the wall?

$$\frac{250\%}{100} = 2.5 \leftarrow \text{scale factor}$$

diameter: $10 \text{ cm} \times 2.5 = 25 \text{ cm}$

height: $12.5 \text{ cm} \times 2.5 = 31.25 \text{ cm}$

or

$$k = \frac{\text{scale}}{\text{original}} \rightarrow \frac{2.5}{1} = \frac{x}{10} \quad \begin{array}{l} x = 2.5(10) \\ x = 25 \text{ cm} \end{array}$$

Example 3:

Tony drew a scale diagram of his new skateboard to show a friend. He used a scale factor of 0.4. The scaled diagram has dimensions 3.2 in. by 1.8 in. by 10.8 in. What are the dimensions of the skateboard?

$$k = \frac{\text{scale}}{\text{original}}$$

$$0.4 = \frac{3.2 \text{ in}}{x}$$

$$\frac{0.4x}{0.4} = \frac{3.2}{0.4}$$

$$x = 8 \text{ in}$$

$$0.4 = \frac{1.8 \text{ in}}{x}$$

$$x = \frac{1.8}{0.4}$$

$$x = 4.5 \text{ in}$$

$$0.4 = \frac{10.8 \text{ in}}{x}$$

$$x = \frac{10.8}{0.4}$$

$$x = 27 \text{ in}$$